

## Seminar 3

### Problem 1

Consider a society with 2 individuals. Assume that the regulator has normative views represented by a classical utilitarian social welfare function:

$$(1) W = U_1 + U_2$$

where  $W$  is the regulator's view of social welfare, and  $U_i$  is person  $i$ 's utility. Moreover, let individual utility be given by

$$(2) U_i = a \ln x_i + b_i \ln E$$

Here,  $x_i$  is person  $i$ 's private consumption, while  $E$  is environmental quality (which is a pure public good).

The regulator is considering whether to go through with a project which will improve the environmental quality by  $dE=1$ . The total cost of this change is  $C=3$ . If the project is implemented, this cost will be distributed equally between the two consumers, so that each pays  $C_i=1.5$ . Let initial environmental quality be  $E=100$ , and the utility parameter  $a=1$ . Lump-sum transfers or side payments are not feasible.

- Assume first that  $b_i=2$  for both individuals. Assume, moreover, that each person's initial private consumption level is 100. Calculate each person's willingness to pay for the environmental improvement associated with the project (assume that the project is marginal, and measure WTP in units of the private consumption good). Will the project be a Pareto improvement? Assume that the regulator knows individuals' WTP. Will the project pass the Hicks-Kaldor-test? Will it increase social welfare, according to the regulator's view?
- Assume now that initial consumption levels differ between persons, and equals 50 for person 1 and 150 for person 2. What is WTP for each person now? Is the project a Pareto improvement, if the costs are still shared equally? Will the project pass the Hicks-Kaldor test? Will it improve social welfare? Give an intuitive explanation for your results, as compared to the results in a).
- Assume now that initial consumption levels differ as described in b), and that, in addition,  $b_i$  differs between individuals in the following way:  $b_1=2$ ,  $b_2=3$ . Costs are still to be shared equally. Will the project now be a Pareto improvement? Will it pass the Hicks-Kaldor-test? Will it improve social welfare? Explain your results intuitively.
- Assume now that the regulator knows neither the utility functions and its parameters, nor the WTP of each individual. Assume that the environmental change from the project discussed above is a decrease in outdoor noise levels in a densely populated area. Discuss which valuation techniques might be used to assess individuals' WTP in this case.

- e) If the environmental change under consideration is, instead, an increase in the population of an endangered bird species in a remote, protected bird reserve without public access, would that affect your conclusions in d)? Discuss.

## Problem 2

A consumer, Bill, purchases voluntarily a climate ticket to neutralize his extra CO<sub>2</sub> emissions when travelling by air. Assume that the cost of the climate ticket is quite substantial, given Bill's budget. However, Bill does not expect to be able to notice at all the improvement in global climate due to his own purchase of climate tickets. Assume that the initial global climate,  $E^0$ , is considered exogenous by Bill. Can his purchase of climate tickets be explained by the following models?

- a) Bill has preferences for his own private consumption ( $x_i$ ) and a stable global climate ( $E$ ), as follows:

$$U_i = u(x_i) + v(E) + k(E)$$

where  $u$ ,  $v$ ,  $k$  are strictly concave and increasing functions, and  $v(E)$  reflects Bill's own benefits for a stable climate and  $k(E)$  his concern for others.

- b) Bill has preferences for private consumption and social approval, but does not in any way care about the global climate as such. (An informal discussion is sufficient.)